Rcourse:
Basic statistics with R

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Contents

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- 80% patients with treatment recovered whereas only 30% patients without recovered.
- A pessimist would say that this just happened by chance.
- What do you do to convince the pessimist?
- You assume he is right and you show that under this hypothesis the data would be very unlikely.

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- This refutes the pessimist. Statistical language: We reject the null hypothesis on the significance level 5%.
- $p = P($observation and everything more 'extreme' $/\mathrm{H}_0$ is true $)$
- If the p value is over 5% you say you cannot reject the null hypothesis.

Statistical tests in R

There is a huge variety of statistical tests that you can perform in R.
We will cover the most basic ones in this lecture and you can find a non-exhaustive list in your lecture notes.

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- Approximative test but rather robust

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Dataset containing height of martian of different colours.
See the code on the R console.

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We cannot reject the null hypothesis.
It was an unpaired test because the two samples are independent.

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Paired test because some persons will cause more damage to the shoe than others.
See the code on the R console.

We can reject the null hypothesis.

Test for (un)equality of variances

In `t.test()` there is an option `var.equal=`.
This way we can control if the variances between the two samples are assumed to be equal or not. The default value is `FALSE`.

If you have a good biological reason, you can assume that the variances are equal. You can test for equality of variances by applying a variance test with the command `var.test`.
Let's see an example on the R console.

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- Approximative test, see the conditions on the lecture notes

Nominal variables: Example

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contingency <- matrix( c(47,3,8,42,60,15,8,33,3),
nrow=3 )
chisq.test(contingency)$expected
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See on the R console.

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All expected abundances are above 5, so we may apply the test.

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chisq.test(contingency)
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Reject the null hypothesis that the two variables are independent.

Nominal variables: Fishers exact test

In case of 2 by 2 contigency tables the chi square approximation is not needed and we can use the **Fisher's exact test**.

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table <- matrix( c(14,10,21,3), nrow=2 )
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- **Assumption:** x and y are samples from a normal distribution.

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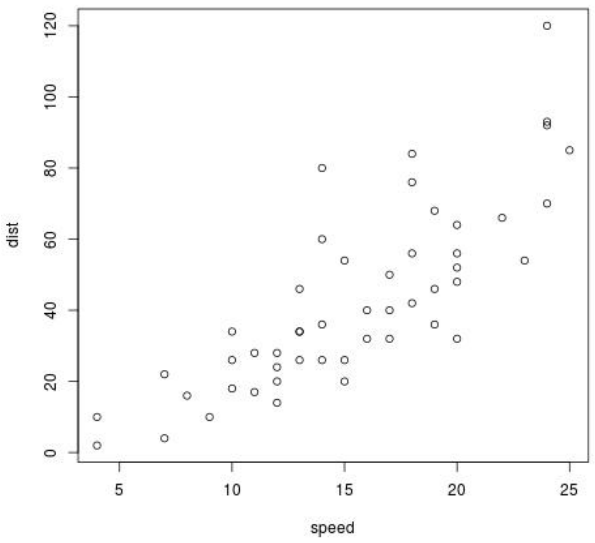
- **Null hypothesis:** x and y are independent
- **Test:** Pearsons correlation test for independence
- **Assumption:** x and y are samples from a normal distribution.
- **R command:** `cor.test(x,y)`

Continuous variables: Example

Distance needed to stop from a certain speed for cars. This dataset is pre-installed in R and can be loaded with the command `data(cars)`



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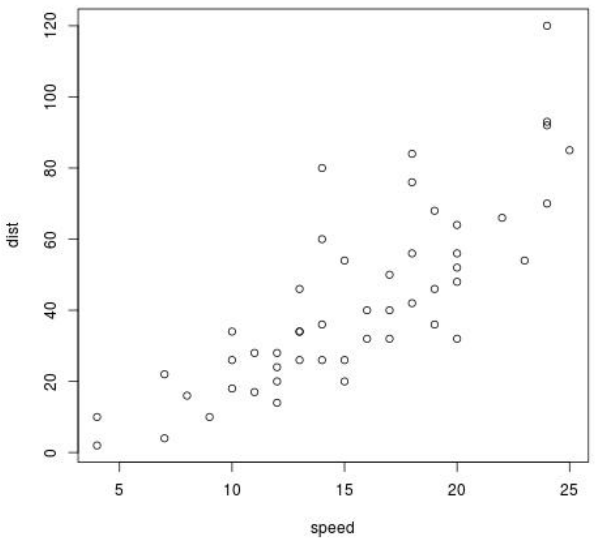

Reject the null hypothesis that the correlation is equal to 0.

Testing for neutrality

The Pearsons correlation assumes normal distrubition of the variables.
When this is not true you can modify the option `method = "pearson"` to use another type of correlation test (Kendall or Spearman).

If you want to test for deviation from the normality you can apply a Shapiro test with the command `shapiro.test`.
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The measure of speed does not deviate significantly from normality, but the distance variable does deviate.

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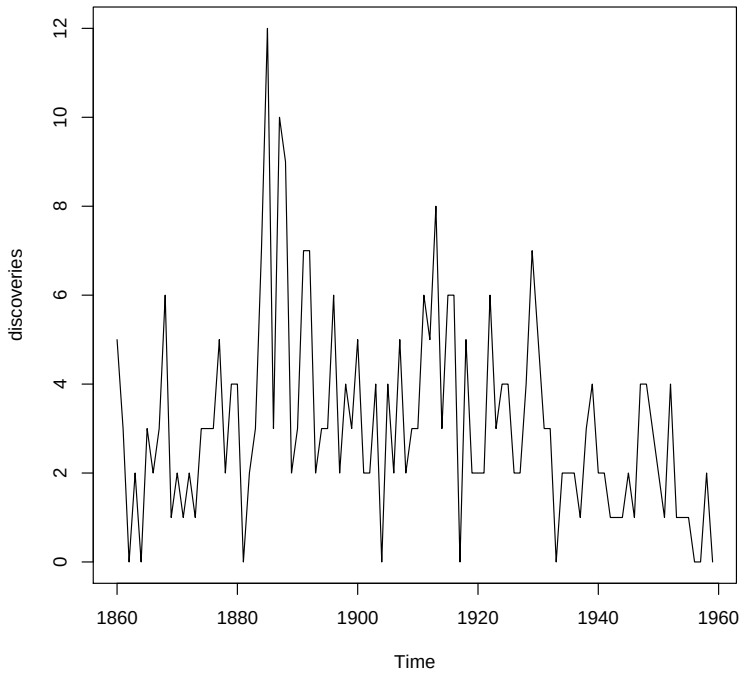
- **Null hypothesis:** x and y are uncorrelated
- **Test:** spearmans rank correlation rho
- **R command:** `cor.test(x,y, method="spearman")`

Ordinal variables: Example

Number of important scientific discoveries or inventions per year. This dataset is pre-installed in R and can be loaded with the command `data(discoveries)`



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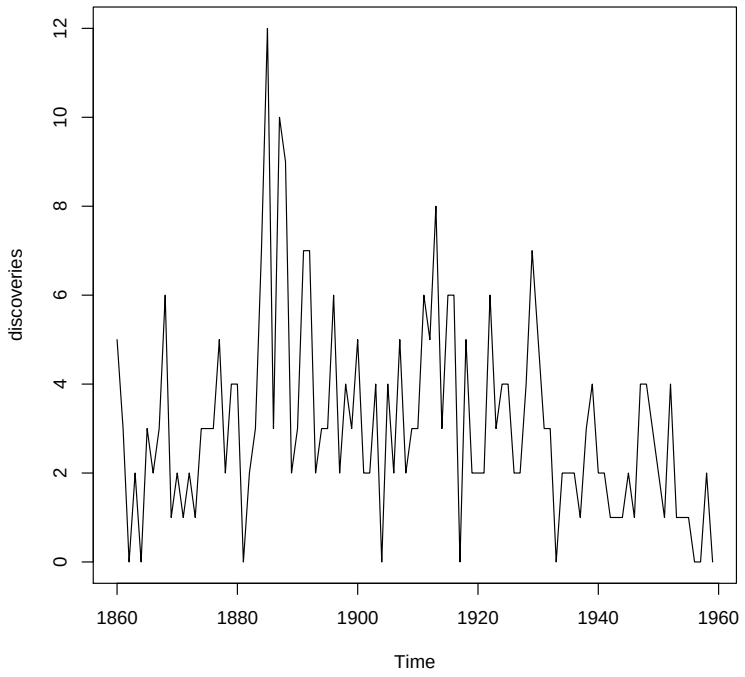

Reject the null hypothesis that the correlation is equal to 0. There is a significant negative correlation.

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Power of a test = 1 - β
If power=0: you will never reject H_0.
The choice of H1 is important because it will influence the power.
In general the power increases with sample size.

Power in R

Use the functions `power.t.test()` or `power.fisher.test()` (in package statmod) to calculate the minimal sample size needed to show a certain difference.
We will try this during the exercise session.

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Definition: degrees of freedom of a sample = the sample size minus the number of parameters estimated from the sample.